TAM251_Chapter8_CombinedLoading_prelecture_Johnso...

Chapter 8: Combined Loading

Chapter Objectives

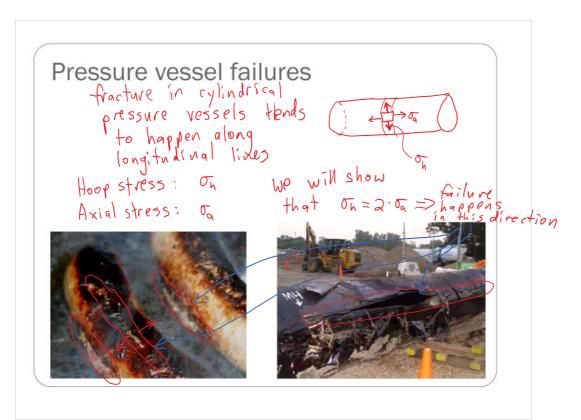
- ✓ Determine stresses developed in thin-walled pressure vessels
- ✓ Determine stresses developed in a member's cross section when axial load, torsion, bending and shear occur simultaneously.

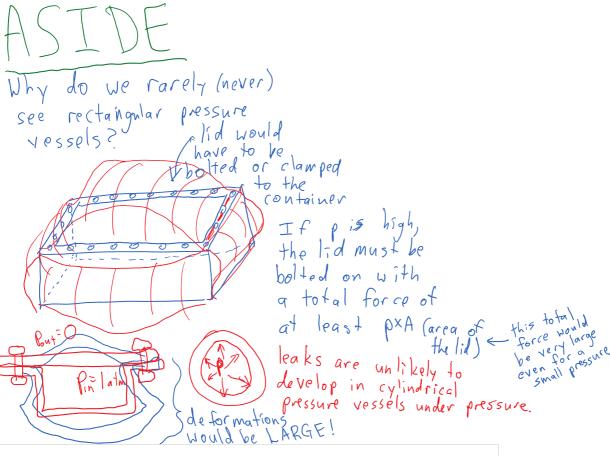
Thin-walled pressure vessels

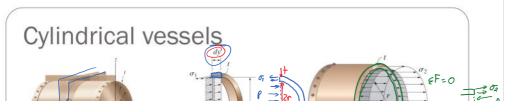
- Inner radius: r
- Wall thickness: t
- Thin walls: $\frac{r}{t} \ge 10$
- Assume that stress distribution in thin wall is uniform
- Pressure vessel contains fluid under pressure p

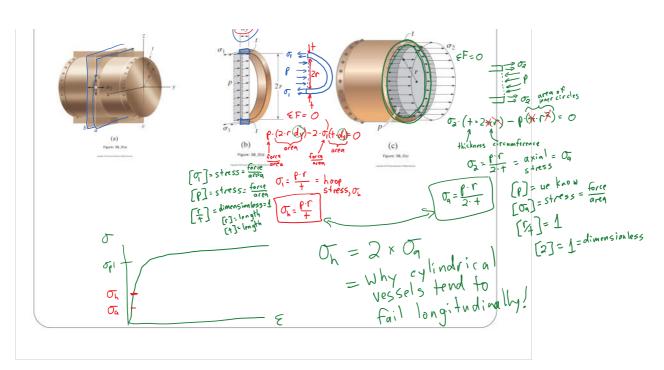


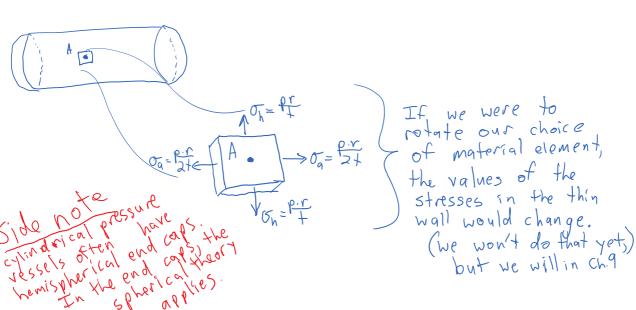
Spherical vessels

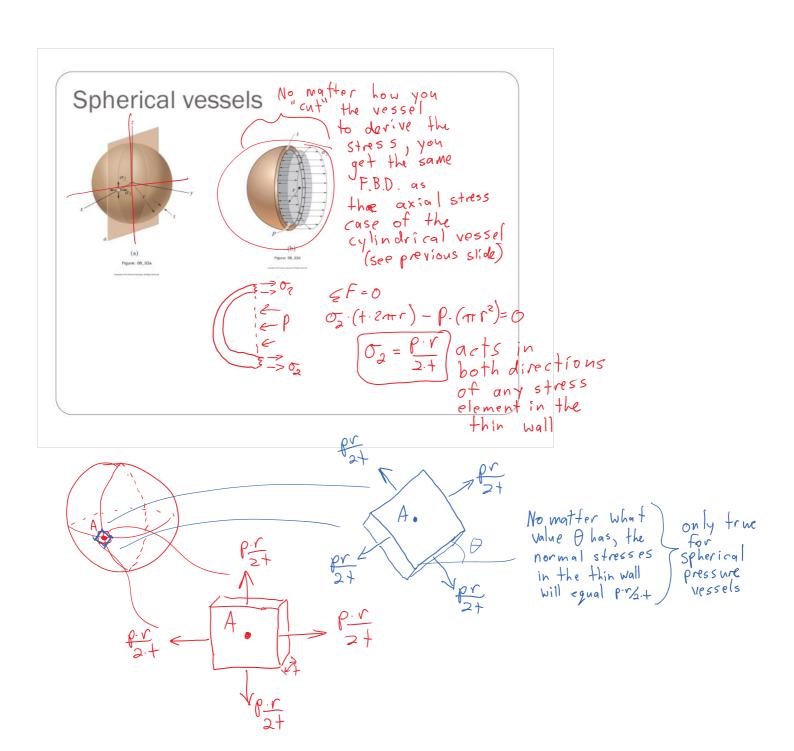












Example: A spherical pressure vessel of D = 900-mm outer diameter is to be fabricated from a steel having an ultimate tensile stress $\sigma_{u} = 400 \, \text{MPa}$. Knowing that a factor of safety of FS=4.0 is desired and that the gage pressure can reach $\rho = 3.5 \, \text{MPa}$, determine the smallest wall thickness that should be used. $\rho = \rho_{\text{gage}} = \rho_{\text{inner}} - \rho_{\text{outer}}$ $\rho_{\text{outer}} - \rho_{\text{outer}} - \rho_{\text{outer}}$ $\rho_{\text{atm}} = 1 \, \text{other}$ $\rho_{\text{atm}} = 1 \, \text{other} = 10^{6} \, \text{ps} = 10^{3} \, \text{ps} = 1$

- Torsional moment T (circular shafts) leads to shear stress varying in the cross-section $\, au=\,$
- Shear force V (beam 5) where the shear stress varying in the cross-section $\tau = \frac{VQ(\gamma)}{V}$
- Bending moment M

 leads to normal stress varying in the cross-section $|\sigma| =$
- Internal pressure p in a spherical or cylindrical vessel leads to hoop stress $\sigma_h = \frac{pr}{t}$ and axial stress $\sigma_a = \frac{pr}{2t}$

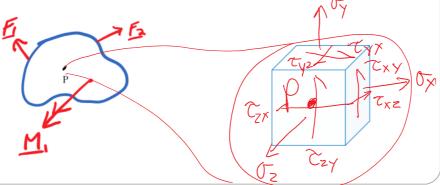
Q(1) Job langest at N.A.

State of stress in a solid

Consider a solid body subjected to externally applied loads

Suppose we wish to know about the stresses being caused at a particular point of interest, point P.

We can draw a small (infinitesimal) cube of material around the point of interest and note the infinitesimal forces that act on each face. In general, the force acting on each face can be broken into 3 vector components, one of which is normal to the face and two of which act in the plane of the face



Stress in 2 and 3 dimensions

Normal stresses: σ_x , σ_y , σ_z

Shear stresses: $\tau_{xy} = \tau_{yx}$, $\tau_{yz} = \tau_{zy}$, $\tau_{xz} = \tau_{zx}$ \rightarrow equalities due to requirement of zero net moment in equilibrium

First index: indicates face normal direction

Second index: indicates force direction on that face

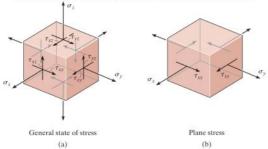
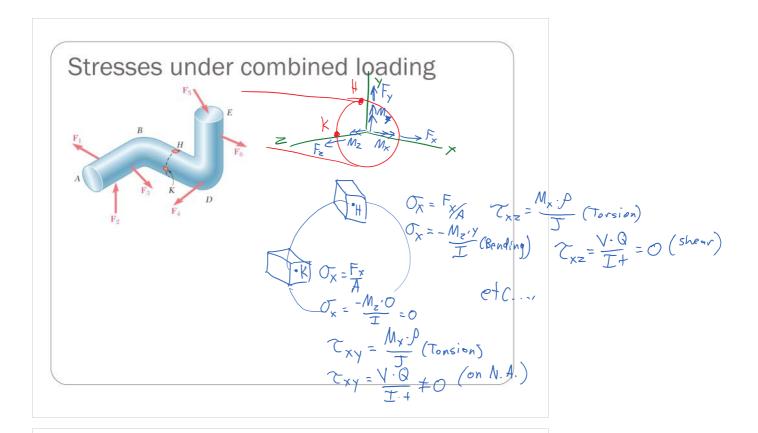
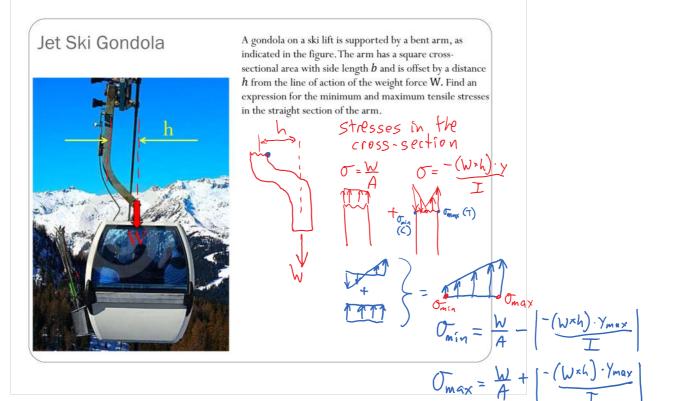


Figure: 09_01

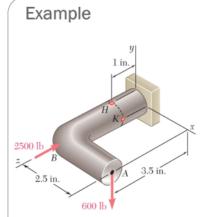






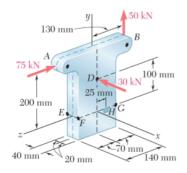
Find the state of stress at points H and K





Find the state of stress at points \boldsymbol{H} and \boldsymbol{K}

Example



Three forces are applied to a short steel post as shown. Determine the state of stress at point ${\cal H}$ on the outer surface of the post.